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A NOVEL MULTICLASS SUPPORT VECTOR MACHINE ALGORITHM USING MEAN REVERSION AND COEFFICIENT OF VARIANCE

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ABSTRACT

Inaccuracy of a kernel function used in Support Vector Machine (SVM) can be found when simulated with nonlinear and stationary datasets. To minimise the error, we propose a new multiclass SVM model using mean reversion and coefficient of variance algorithm to partition and classify imbalance in datasets. By introducing a series of test statistic, simulations of the proposed algorithm outperformed the performance of the SVM model without using multiclass SVM model.

Keywords: Support Vector Machine, Multiclass, Mean Reversion, Coefficient of Variance

1. INTRODUCTION

1.1. Background on Mean Reversion and Coefficient of Variance

There are many definitions of mean reversion. In general, it is an asset model, which shows that the asset price tends to fall (or rise) after hitting a maximum (or minimum). The process of mean reversion is a lognormal diffusion, but the variance does not growing in proportion to the time interval (Pillay and O'Hare, 2011). The variance grows at the start and sometimes it stabilises at a certain value. The most basic mean reversion model is the (arithmetic) (Uhlenbeck and Ornstein, 1930). This model is a stochastic process with stationary, Gaussian and Markovian distribution and use to describe the velocity of a massive Brownian particle under the influence of friction. In the other approach, Zhao et al. (2011) introduced AR process where the value drifted to its mean in the long run. Currently, two main methodologies are used for measuring the mean reversion, i.e., (i) variance ratio and (ii) regression. Cochrane (1988) has used the variance ratio to measure the relative importance of the random walk component.

Poterba and Summers (1988) and Lo and Mackinlay (1988) compared the relative variability of returns over different time horizons using the variance ratio in discrete time series. Bali and Demirtas (2008) confirmed these reports by showing that in a 'high variance' scenario and using the mean reversion concept could cause negative drift. Using regression tests, Fama and French (1992) determined the correlation with currency asset returns, while Chen and Jeon (2000) measured its mean reversion behaviour and found that the returns were positively autocorrelated over shorter periods but negatively autocorrelated over longer periods. To measure imbalance in multiclass datasets, Cieslak and Chawla (2009) recommended to use Coefficient of Variance to solve the problem. Diebold (2004) also reported mean reversion using fractional unit-root analysis of real exchange rates under the gold standard. Diebold (2004) showed that the power of the test for mean reversion could be raised.

1.2. Background on One-Against-All and One-Against-One Strategies

tio to measure The two commonly used simple decomposing lk component. (i) One-against-all approach constructs

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binary SVM classifiers, each of which separates one class from all the rest. The SVM is trained with all the training examples of a class with positive labels and all the others with negative lables; and (ii) the "One-Against-One", which builds one SVM for each pair of 2009). More complex (Chen et al., classes decomposition methods employing Error Correcting Output Codes (ECOC) have been introduced (Dietterich and Bakiri, 1995; Allwein et al., 2005). Hsu and Lin (2002) compared several multiclass SVM methods. The conclusion from their works is that "One-Against-One" is more practical, because the training process is quicker. Rifkin and Klautau (2004) disagreed with Allwein et al. (2005) that "One-Against-One" and other ECOC were more accurate than the "One-Against-All" strategy, arguing that the "One-Against-All" strategy war as accurate as any other approach by assuming that the SVMs are well tuned. Rifkin and Klautau (2004) concluded that a simple scheme such that One-Against-All and One-Against-One was preferable to a highly complex ECOC methods.

1.3. Background on the EMD Algorithm

The analysis of nonlinear and nonstationary data is important in many applications such as bioinformatics (Shi et al., 2008; Huang et al., 1996), signal processing (Huang et al., 1998; Huang and Attoh-Okine, 2005; Huang and Shen, 2005), geophysics (Wang et al., 1990; Datig and Shlurmann, 2004) and finance (Huang and Attoh-Okine, 2005; Guhathakurta et al., 2008). Huang et al. (1996) formulated an a posteriori algorithm with adaptive control over a separate data structure, which was later termed the Hilbert-Huang Transform (HHT) (Huang et al., 1998). The HHT overcomes the limitations of the Hilbert transform, which is only suitable for a narrow band-pass signal. The key element of the HHT algorithm is the EMD, in which any complicated dataset can be decomposed into a finite and often small number of Intrinsic Mode Functions (IMFs) that allow a well-behaved Hilbert transform. Since this decomposition is based on the local characteristic time scale of the data, it is applicable to nonlinear and nonstationary processes (Huang and Attoh-Okine, 2005). In signal processing, high-frequency noises from input data are considered simple intrinsic mode oscillations (Huang and Attoh-Okine, 2005). The EMD uses a sifting process and curve spline technique to decompose a signal into a new oscillatory signal termed the IMF. After a number of decomposition iterations, the characteristics of the IMF must meet two conditions. First, in the entire dataset the number of extrema (maxima plus minima) and number of zero crossings must either be the same or differ by at most one. Second, at any point the mean values of the envelopes defined by the local maxima and the local minima must be zero (Huang and Shen, 2005). The EMD algorithm, which is fundamental to the HHT, can thus reduce high-frequency noise from input data, such as noise from retail trades on a stock exchange.

1.4. Objective

This study presents a novel multiclass SVM model using mean reversion and coefficient of variance algorithm to partition and classify the datasets; and then introduce SVM to measure their performance. For verification, we compared to the multiclass SVM model with another SVM model that was without mean reversion and coefficient of variance algorithm.

2. MATERIALS AND METHODS

2.1. SVM Model

There are several methods used for data classification, one of them being SVM. Let x be a vector in a vector space. A boundary hyperplane is expressed as one of the hyperplanes:

$$w^{\mathrm{T}}x + b = 0 \tag{1}$$

Where:

w = A weight coefficient vector and

b = A bias term. The distance between training vectors

 x_i = The boundary, called margin, is expressed as follows:

$$\frac{\left\|\mathbf{w}^{\mathrm{T}}\mathbf{x}_{\mathrm{i}}+\mathbf{b}\right\|}{\left\|\mathbf{w}\right\|} \tag{2}$$

Since the hyperplanes expressed by Equation 1 where w and b are multiplied by a common constant are identical, we introduce a restriction to this expression, as follows Equation 3:

$$\min_{i} \left| \mathbf{w}^{\mathrm{T}} \mathbf{x} + \mathbf{b} \right| = 1 \tag{3}$$

The optimal boundary maximizes the minimum of Equation 2. By the restriction of Equation 3, this is



reduced to maximisation of $\frac{1}{\|\mathbf{w}\|^2} = \frac{1}{\mathbf{w}^T \mathbf{w}}$. As a result, the

underlying optimisation is formalised as Equation 4:

Minimize
$$w^T w$$
 (4)

subject to $y_i (w^T x + b) \ge 1$.

where, y_i is 1 if x_i belongs to one set and y_i is-1if x_i belongs to the other set. If the boundary classifies the vectors correctly, then y_i (w^Tx+b) ≥ 0 , of which it is identical to the margin.

This conditional optimisation is achieved by Lagrange's method of indeterminate coefficient. Define a function:

$$L(\mathbf{w}, \mathbf{b}, \boldsymbol{\alpha}_{i}) = \frac{1}{2} \mathbf{w}^{\mathrm{T}} \mathbf{w} - \sum_{i} \boldsymbol{\alpha}_{i} \left[\mathbf{y}_{i} \left(\mathbf{w}^{\mathrm{T}} \mathbf{x} + \mathbf{b} \right) - 1 \right]$$
(5)

where, $\alpha_i \ge 0$ are the indeterminate coefficients. If w and b take the optimal value, the partial derivatives are zero:

$$\frac{\partial L}{\partial w} = w - \sum_{i} \alpha_{i} y_{i} x_{i}, \frac{\partial L}{\partial b} = -\sum_{i} \alpha_{i} y_{i}$$
(6)

By setting the derivatives of Equation 6 to zero, we obtain:

$$w = \sum_{i} \alpha_{i} y_{i} x_{i}$$
⁽⁷⁾

$$\sum_{i} \alpha_{i} y_{i} = 0 \tag{8}$$

Rewriting Equation 5, we obtain:

$$L(\mathbf{w},\mathbf{b},\alpha_{i}) = \frac{1}{2}\mathbf{w}^{\mathrm{T}}\mathbf{w} - \sum_{i}\alpha_{i}\mathbf{y}_{i}\mathbf{w}^{\mathrm{T}}\mathbf{x}_{i} - \mathbf{b}\sum_{i}\alpha_{i}\mathbf{y}_{i} + \sum_{i}\alpha_{i}, \qquad (9)$$

Substituting Equations 7-9, we obtain Equation 10:

$$L(\mathbf{w}, \mathbf{b}, \boldsymbol{\alpha}_{i}) = \frac{1}{2} \left(\sum_{i} \boldsymbol{\alpha}_{i} \mathbf{y}_{i} \mathbf{x}_{i} \right)^{\mathrm{T}} \left(\sum_{j} \boldsymbol{\alpha}_{j} \mathbf{y}_{j} \mathbf{x}_{j} \right)$$
$$- \sum_{i} \boldsymbol{\alpha}_{i} \mathbf{y}_{i} \left(\sum_{j} \boldsymbol{\alpha}_{j} \mathbf{y}_{j} \mathbf{x}_{j} \right)^{\mathrm{T}} + \sum_{i} \boldsymbol{\alpha}_{i}$$
$$= \frac{1}{2} \sum_{i} \sum_{j} \boldsymbol{\alpha}_{i} \boldsymbol{\alpha}_{j} \mathbf{y}_{i} \mathbf{y}_{j} \mathbf{x}_{i}^{\mathrm{T}} \mathbf{x}_{j} + \sum_{i} \boldsymbol{\alpha}_{i}$$
(10)

The contribution of the second term of Equation 5 should be minimised versus L should be maximised



subject to α . Consequently, the optimisation is reduced to a quadratic programming problem as follows:

$$\begin{aligned} \text{Maximize} &-\frac{1}{2} \sum_{i} \sum_{j} \alpha_{i} \alpha_{j} y_{i} y_{j} x_{i}^{\mathrm{T}} x_{j} + \sum_{i} \alpha_{i} \\ \text{subject to} &\sum_{i} \alpha_{i} y_{i} = 0, \ \alpha_{i} \ge 0 \end{aligned}$$
(11)

Let Φ be a transformation to a higher dimensional space. The transformed space should satisfy that the distance is defined in the transformed space and the distance has a relationship to the distance in the original space. The kernel function K(x,x') is introduced for satisfying the above conditions. The kernel function satisfies:

$$\mathbf{K}(\mathbf{x},\mathbf{x}') = \boldsymbol{\Phi}(\mathbf{x})^{\mathrm{T}} \boldsymbol{\Phi}(\mathbf{x}') \tag{12}$$

The above Equation 12 indicates that the kernel function is equivalent to the distance between x and x' measured in the higher dimensional space transformed by Φ . If we measure the margin by the kernel function and perform the optimisation, a nonlinear boundary is obtained. Note that the boundary in the transformed space is obtained as:

$$\mathbf{w}^{\mathrm{T}}\Phi(\mathbf{x}) + \mathbf{b} = 0 \tag{13}$$

Substituting Equation 7 into the above Equation 13 while replacing x with $\Phi(x)$, we obtain:

$$\sum_{i} \alpha_{i} y_{i} \Phi\left(x_{i}^{T}\right) \Phi\left(x\right) + b = \sum_{i} \alpha_{i} y_{i} K\left(x_{i}, x\right) + b = 0$$
(14)

The optimisation function of Equation 11 in the transformed space is also obtained by substituting $x_i^T x_i$ with $K(x_i,x_j)$. These results mean that all the calculation can be achieved by using $K(x_i,x_j)$ only and we do not need to know what Φ or the transformed space actually is.

A sufficient condition for satisfying Equation 14 is that $K(x_i,x_j)$ is positive definite. Several examples of such kernel functions are known, as follows: (Laplacian kernel function) Equation 15:

$$K(x, x') = \exp(-\sigma ||x - x'||)$$
(15)

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2.2. Data Classification Using Mean Reversion and Coefficient of Variance Algorithm

We present a novel multiclass model for use with the SVM family using mean reversion and coefficient of variance algorithm to partition and classify the time horizon (span) of multiclass datasets, respectively. In practice, the typical curve of exchange rates tends to shift towards the mean, so the point of reversal can be used to determine changes in its direction, i.e., from up to down and vice versa. The datasets are then partitioned at the reversal point using the mean reversion algorithm, which later explained, as a decision tool. The standard deviations of a nonstationary datasets are not the same, so we measure the datasets between each reversal points and input them into a SVM model. The procedure for using mean reversion and coefficient of variance algorithm are as follows:

- Compute the mean μ_n (t) of random variables X_n (t)
- Compute the variance $V_n(t)$ of $V_n(t)$
- After normalising each V_n (t) using μ_n (t), we obtain $V_n(t)$
 - $\mu_n(t)$
- In an upward scenario where V₁(t)<V₂(t),..,n or a downward scenario where
- if $\frac{V_2(t)}{\mu_2(t)} < \frac{V_1(t)}{\mu_1(t)}$ or $\frac{V_2(t)}{\mu_2(t)} > \frac{V_1(t)}{\mu_1(t)}$, mark the intercept point on the x-axis and denote it as M₁, i.e., the value is X_m (t) where r =1,2,..,c and c is the last class using coefficient of variance equation ($cv = \frac{\sigma}{\mu}$ where CV is coefficient of variance) or
- if $\frac{V_{n-1}(t)}{\mu_{n-1}(t)} = \frac{V_n(t)}{\mu_n(t)}$, do not use the intercept point on the x-axis
- Repeat 4) and stop when $\frac{V_n(t)}{\mu_n(t)}$ is the last data point
 - (n). Next, plot M_2, \ldots, M_n
- Compute CV for the data X_m (t) in blocks of M_1 , M_2 ,..., M_n where n-1 is the number of partitions/blocks

The original datasets X_n (t) was classified in different classes of coefficient of variance and termed to CV class. The next step aims to simulate X_n (t) individually using the SVM model for each CV group. As a result, these multiple sets of kernel parameters in each SVM simulation are created; we then integrate all the blocks partitioned by the CV.

2.3. Cross Validation Methods

Schneider and Moore (1997) classified model evaluation into many methods, e.g., judging the model quality based on the residuals, black box model selection and cross-validation. According to their reports, crossvalidation is a model evaluation method that separates training and test data, which uses the test data to test the performance after the training data were computed by a statistical model. Cross-validation uses the following three main methods.

2.3.1. Holdout

The Holdout method is the simplest type of crossvalidation. The datasets is separated into two sets: the training set and the test set. The estimation model fits the training set only and leaves the test data blind. The performance of the Holdout method can be quantified using a variety of test statistic, i.e., MSE, MAE, MAPE, R^2 , AIC and BIC. This method is usually preferable to the residual method and it does take that much no longer to compute. However, its evaluation can have a high variance, which may depend greatly on how the training and test data are divided. In this study, we select and divide datasets using different ratios of the training data and test data, i.e., 30:70, 50:50 and 70:30, respectively.

2.3.2. K-Fold

K-fold was proposed to improve the Holdout method. The K-fold method divides the entire datasets into *k* subsets and uses the Holdout method k times. In each subset, the training data are computed using the model and tested with the test data. Thus, the average error is computed across all k trials. The advantage of this method is that it is less important how the data is divided. Every data point is used in the test set exactly once and in a training set k-1 times. The variance of the estimate is reduced to k is increased. The disadvantage of this method is that the training algorithm has to be rerun from scratch k times, which means it requires k times as many computation to make an evaluation. A variant of this method is to randomly divided the data into a test and training set k different times.

2.3.3. Leave-One-Out

The name Leave-one-out explains itself. This method applies bootstrap sampling by taking one particle (data unit) out of the overall training and test datasets whereas



the remaining data are used for reference. The advantage is that the accuracy of the outcome but this is traded-off by the massive computational power requirements when handling large input datasets. Moreover, this method was designed only for model evaluation or in-sample forecasting so it is rather difficult to apply this method to out-of-sample forecasting.

2.4. The OAO and OAA Strategies

In general, the multiclass SVM is an ongoing research issue and it can be fundamentally classified using two different strategies: (i) OAA consists of building one SVM per class and trains it while the rest of the training data remains as the other class so-called 'All'. The method of building the 'One' class is flexible depending upon the structure of datasets and (ii) OAO is similar to the OAA strategy except the 'All' class is individually partitioned into subclasses. The discrimination of OAA strategy between an information class and all others often leads to the estimation of complex discriminant functions (Schneider and Moore, 1997). In brief, the OAO decomposes the original problem into a set of small problems of two information classes with n(n-1)/2 binary SVMs. In this study, we have selected mean reversion and coefficient of vraince algorithm for selecting the training data.

3. RESULTS

The simulations were conducted on a personal computer with clock frequency at 2.50GHz, Intel® core^(TM) i5-3210 M CPU and 8 GB of RAM. All the SVMs were trained with R programming software (Kim and Oh, 2012). We use all kernel functions i.e., Gaussian, polynomial, linear, Laplace, Bessel and ANOVA RBF; then, select the best performance out of those functions.

With respect to Materails and Methods, we introduced theoretical considerations related to the SVM model and its background in supervised learning and its structure risk minimisation. We also selected the Holdout model, which is part of the model evaluation used to segregate training and test datasets, before partitioning them using the mean reversion and coefficient of variance algorithm. This technique is novel and it is used to construct a multiclass for the SVM family.

3.1. Simulation Procedure

We describe the simulation procedure used by the multiclass SVM model, as shown in **Fig. 1**. The systematic order of the workflow is as follows:

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- Retrieve 2322 datasets, EUR-USD exchange rates from Bloomberg terminal from 2001 to 2011
- Demonstrating in **Fig. 1**, we use the Holdout method to separate the datasets into the training and test data. After separation, each group has a ratio of 30:70, 50:50 and 70:30. The 30% of the datasets are used as out-of-sample forecasting
- At the reversal point of the curves resulted from the mean reversion technique described in 2.2, we use CV to classify each group of dependent variables and yields a number of sub-groups
- From (3) for each sub-group we simulate the multiclass SVM model using the R programming software (Kim and Oh, 2012). This fits the multiclass kernel functions and parameters for each subgroup. During this stage, we obtain many kernel parameters for each group partitioned, as shown in **Table 1**
- Integrate all of the results from (4) in the time series domain. Finally, we produce a new classified datasets.
- Quantify the performance of the multiclass SVM model using a variety of test statistic, i.e., MSE, MAE, MAPE, R², AIC, BIC and Accuracy counts which measures upward and downward movements of each local data point of the newly simulated datasets
- Robustness test of the Multiclass SVM model with OAA and OAO strategies: From (3) and Table 1, we assign the first CV class to 'One' and the remaining classes to 'All' as per the OAA strategy. Additionally, we select the second CV class and assign to 'One' and the remaining classes to 'All' and so on. Alternatively, we introduce OAO strategy; thus, the pairing of multiclass is as follows:
 - a) Class 1 and Class 2, Class 1 and Class 3,..., Class 1 and n where n is the last Class
 - b) Class 2 and Class 3, Class 2 and Class 4,...,Class 2 and Class n; until the final when
 - c) Class n-1 and Class n
- For the One-Against-All strategy, we compare simulation results of the data points, which are located in the correct classes with the results from (5); and then analyse the percentage of error. For the One-Against-One strategy, use the outcomes from each paring to vote for the best performance in each class

3.2. Simulation Results

Using procedures in 3.1, we retrieved the original datasets. The next step was to introduce the Holdout method to segregate the training and test data using

different ratios, i.e., 30:70, 50:50 and 70:30. We introduced the mean reversion and coefficient of variance algorithm to partition and classify the training data, respectively. We intended to leave the test data to be used as reference in order to compare with the predicted outcome from the SVM simulation. As a result, 48 blocks/partitions were separated into six CV classes, at which are shown in **Table 1**. We then grouped each CV class and simulated them with the SVM classification model using R Programming scripts (Kim and Oh, 2012). The simulated are shown in **Table 2-6**.

Table 1 was used to plot a graph and **Fig. 2** illustrates the distribution of the six CV classes where the *x*-axis represented 50 blocks/partitions and the *y*-axis represented the CV values of the different classes. The figures in brackets show the number of data points per CV class and they were re-displayed in **Table 4**. Each block/partition contained different numbers of data points, depending on the change in the curve direction, i.e., upward to downward or vice versa.

At this point, we had classified datasets into multiclass. The next step was to run simulations of the SVM models. The results of those simulations are in **Table 3**.

We fitted the kernel distribution functions and their parameters. The outcomes shown in **Table 2** using different sets of kernel functions, i.e., radial, polynomial, linear, Laplacian, hyperbolic, Bessel and ANOVA RBF, were different. Moreover, the number of support vectors, parameters and training error were presented in **Fig. 2**. Definitions of the parameters given in the **Table 2** are as follows:

- Sigma: the inverse kernel width used by the Radial, Gaussian, Laplacian, Bessel and ANOVA RBF kernel functions
- Degree: the degree of the polynomial, Bessel or ANOVA RBF kernel functions, i.e., a positive integer
- Scale: the scaling parameter of the polynomial and tangent kernel functions is a convenient way of
- normalising patterns without any need to modify the data itself
- Offset: the offset used in polynomial or hyperbolic tangent kernel functions
- Order: the order of the Bessel function

Next, we used the test statistic, i.e., MSE, MAE and MAPE, to measure the performance of each kernel function in all CV classes of the datasets. The results given in **Table 3** show that the Laplacian kernel functions performed the best. Having successfully simulated the SVM with



Laplacian kernel functions and parameters, in conclusion there were six CV classes in 48 blocks/partitions and each block had a different number of data points.

Table 4 shows the CV classes including the Laplacian kernel functions and parameters. At this stage, we completed simulations required for building up the training data.

Referring to the SVM model for classification, we simulated the test data, which came from the ratio of training and test data at 70:30, by using the trained Laplacian kernel functions and their parameters. The simulation results of the three datasets shown in **Fig. 3**, at which the *x*-axis represented the number of data points used for classification and the *y*-axis represented the EUR-USD. Finally, the results demonstrated that the graph of the multiclass SVM model in black solid line agreed with the graph of the original datasets in dotted blue line, whereas the graph of SVM model only was deviated from those two graphs. To ease for presentation, the x-axis represented the test data ranking between 2001st to 2049th of the original datasets.

To verify the performance of the multiclass using the mean reversion and coefficient of variance algorithm, we plotted three graphs, which showed the simulation results for the multiclass SVM model and the SVM without multiclass algorithm (SVM model only). The two graphs of the SVMs after simulations with and without multiclass were significantly different, as shown in Table 5. Using the Laplacian kernel function and a training:test data ratio of 70:30. For example, we compared the Accuracy count which was 79.88%, whereas the SVM model without the multiclass algorithm measured by Accuracy count of 73.21%. Finally, we measured the performance of the multiclass SVM model comparing with the SVM model only by using the test statistic, i.e., MSE, MAE, MAPE, R^2 , AIC and BIC. The results in Table 5. showed that the proposed model outperformed the performance of the simulation from the SVM model only.

3.3. Robustness Test

We reintroduced the same R Programming software application, which was used to generate the results shoewn in the figures indicated in the **Table 3-4**, to simulate the OAA and OAA strategies. The simulation procedure was similar to the procedures in 3.1 of which the input data were four different exchange rates, namely; EUR-USD, EUR-CNY, EUR-RUB and EUR-CHF. It is noted that each input dataset contained 2322 data point retrieved from Bloomberg terminal from 2001 to 2011.

Block no.	Rankin	CV class number	No. of data point	CV value
1	1^{st} to 12^{th}	2	12	0.02592
2	13^{th} to 16^{th}	1	4	0.02278
3	17^{th} to 23^{rd}	2	7	0.02592
4	24^{th} to 25^{th}	1	2	0.02278
5	26^{th} to 26_{th}	2	1	0.02592
6	27^{th} to 38^{th}	1	12	0.02278
7	39^{th} to 46^{th}	2	8	0.02592
8	47^{tr} to 181^{st}	1	135	0.02278
9	182 nd to 184 nd	2	3	0.02592
10	185^{m} to 361^{m}	1	1//	0.02278
11	502 t0 504 $505^{\text{th}} to 505^{\text{th}}$	2	145	0.02392
12	505 th to 505 th	2	1	0.02592
14	500^{th} to 500^{rd}	3	97	0.02077
15	604^{th} to 656^{th}	4	53	0.05361
16	657 th to 657 th	3	1	0.02077
17	658^{th} to 658^{th}	2	1	0.02592
18	659^{th} to 680^{th}	4	22	0.05361
19	681 st to 696 th	3		0.02077
20	697^{th} to 701^{st}	4	5	0.05361
20	702^{nd} to 702^{nd}	3	1	0.02077
21	702^{rd} to 1748^{th}	3	1016	0.02077
22	$1740^{\text{th}} + 1740^{\text{th}}$	4	1040	0.03301
23	1749 to 1749	5	1	0.01840
24	1/50 to 1/50	4	1	0.05361
25	1/51 st to 1/59 st	5	9	0.01840
26	1760 th to 1760 th	4	1	0.05361
27	1761^{st} to 1861^{st}	5	101	0.01840
28	1762 nd to1978 th	6	217	0.01259
29	1980^{th} to 2001^{st}	5	22	0.01840
30	$2002^{\rm nd}$ to $2003^{\rm rd}$	4	2	0.05361
31	2004 th to 2016 th	5	13	0.01840
32	2017^{th} to 2071^{st}	4	55	0.05361
33	2072^{nd} to 2073^{rd}	5	2	0.01840
34	2074^{th} to 2188^{th}	4	115	0.05361
35	2089^{th} to 2193^{rd}	5	105	0.01840
36	2104^{th} to 2107^{th}	4	4	0.05361
27	2194 to 2197	+ 5	4	0.05501
57	2198 to 2198	5	1	0.01840
38	2199 th to 2211 th	4	13	0.05361
39	2212 th to 2212 th	5	1	0.01840
40	2213 th to 2221 st	4	9	0.05361
41	2222^{nd} to 2231^{st}	5	10	0.01840
42	2232 nd to 2233 rd	4	2	0.05361
43	2234 th to 2244 th	5	11	0.01840
44	2245 th to 2245 th	4	1	0.05361
45	2246 th to 2316 th	5	71	0.01840
46	2317^{th} to 2317^{th}	6	1	0.01259
47	2318 th to 2320 th	5	3	0.01840
48	2321 st to 2322 nd	6	1	0.01250

 Table 1. Classification of the CV class ranking for each block, the CV and their related values and the number of blocks created by mean reversion algorithm

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Class of Isomal	No. of	ev cluss					Obiastiva	Training
Class of Kernel	INO. 01	C :	Desires	C1-	Off	Outen	Objective	Training
Tunctions	support vectors	Sigma	Degree	Scale	Ollset	Order	function value	error
Radial		0.00					10.70	0.00
1	77	0.09	N.A.	N.A.	N.A.	N.A.	-18.62	0.02
2	53	0.16	N.A.	N.A.	N.A.	N.A.	-13.34	0.03
3	38	0.17	N.A.	N.A.	N.A.	N.A.	-7.91	0.01
4	265	0.12	N.A.	N.A.	N.A.	N.A.	-46.51	0.01
5	51	0.44	N.A.	N.A.	N.A.	N.A.	-27.54	0.12
6	28	0.07	N.A.	N.A.	N.A.	N.A.	-12.14	0.05
Polynomial								
1	53	N.A.	1.00	1.00	1.00	N.A.	-13.50	0.03
2	30	N.A.	1.00	1.00	1.00	N.A.	-9.51	0.03
3	23	N.A.	1.00	1.00	1.00	N.A.	-2.26	0.01
4	196	N.A.	1.00	1.00	1.00	N.A.	-108.63	0.13
5	40	N.A.	1.00	1.00	1.00	N.A.	-38.47	0.41
6	23	N.A.	1.00	1.00	1.00	N.A.	-4.87	0.03
Linear								
1	53	N.A.	N.A.	N.A.	N.A.	N.A.	-13.50	0.03
2	30	N.A.	N.A.	N.A.	N.A.	N.A.	-9.51	0.03
3	23	N.A.	N.A.	N.A.	N.A.	N.A.	-2.26	0.01
4	196	N.A.	N.A.	N.A.	N.A.	N.A.	-108.63	0.13
5	40	NA	NA	NA	NA	NA	-38.47	0.41
6	23	N A	N A	N A	N A	N A	-4.87	0.03
Lanlacian	25	11.71.	1 1.7 1.	11.11.	11.71.	1 4.7 1.	4.07	0.05
1	73	0.08	ΝΔ	ΝΔ	ΝΔ	ΝΔ	-26.78	0.02
2	12	0.13	N A	N A	N A	N A	_17.01	0.02
23	30	0.15	N.A.	N.A.	N.A.	N.A.	-17.01	0.00
1	37	0.19	N.A.	NA.	N.A.	N.A.	-9.07	0.01
4	312	0.12	IN.A.	IN.A.	IN.A.	IN.A.	-39.43	0.01
5	40	0.10	N.A.	N.A.	N.A.	IN.A.	-55.79	0.23
0	25	0.09	N.A.	N.A.	N.A.	N.A.	-10.70	0.17
Hyperbolic	40	NT A	NT A	1.00	1.00	NT A	121 65	110.20
1	49	N.A.	N.A.	1.00	1.00	IN.A.	-431.03	110.29
2	20	N.A.	N.A.	1.00	1.00	N.A.	-140.27	51.68
3	18	N.A.	N.A.	1.00	1.00	N.A.	-48.33	12.76
4	188	N.A.	N.A.	1.00	1.00	N.A.	-/391.51	23/3.01
5	36	N.A.	N.A.	1.00	1.00	N.A.	-197.83	65.98
6	19	N.A.	N.A.	1.00	1.00	N.A.	-53.53	16.25
Bessel								
1	70	1.00	1.00	N.A.	N.A.	1.00	-29.68	0.07
2	41	1.00	1.00	N.A.	N.A.	1.00	-15.55	0.07
3	28	1.00	1.00	N.A.	N.A.	1.00	-8.57	0.02
4	41	1.00	1.00	N.A.	N.A.	1.00	-15.55	0.07
5	42	1.00	1.00	N.A.	N.A.	1.00	-32.32	0.21
6	29	1.00	1.00	NA	NA	1.00	-12.95	0.07
ANOVA RRE		1.00	1.00	1 1.2 1.	1 1.1 1.	1.00	12.70	0.07
1	02	1.00	1.00	ΝA	ΝA	N A	10.62	0.01
2	5 <u>2</u> 60	1.00	1.00	N A	IN.A.	IN.A.	-10.02	0.01
∠ 2	50	1.00	1.00	IN.A.	IN.A.	IN.A.	-5.42	0.01
3	50	1.00	1.00	IN.A.	IN.A.	IN.A.	-2.55	0.00
4	50	1.00	1.00	N.A.	N.A.	N.A.	-2.53	0.00
5	56	1.00	1.00	N.A.	N.A.	N.A.	-18.71	0.06
6	44	1.00	1.00	N.A.	N.A.	N.A.	-4.81.00	0.01

 Table 2. Kernel functions for each CV class

Table 3. Performance evaluation for all kernel functions

Kernel function	MSE	MAE	MAPE
Radial	3.84E-05	0.0048831	0.375369
Polynomial	0.000520	0.0159646	1.212167
Linear	0.000520	0.0159676	1.212442
Laplacian	3.24E-05	0.0046254	0.360253
Hyperbolic	6.192284	1.5028091	113.5211
Bessel	0.000483	0.0128695	0.985140
ANOVA RBF	0.000103	0.0072116	0.547114



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Table 4. Details of the number of blocks per CV class, the parameters of the CV class and its value				
Class	Blocks	Parameter of Laplacian kernel function	CV	
1	5	$F(w,x) = w^{T} \exp(-0.880257537388077 x-x')+b$	0.02278	
2	8	$F(w, x) = w^{T} \exp(-0.126109678105003 x-x')+b$	0.02592	
3	5	$F(w, x) = w^{T} \exp(-0.1872440577155 x-x')+b$	0.02077	
4	14	$F(w, x) = w^{T} \exp(-0.120770384940063 x-x') + b$	0.05361	
5	13	$F(w, x) = w^{T} \exp(-0.156375637970856 x-x')+b$	0.01840	
6	3	$F(w, x) = w^{T} \exp(-0.880257537388077 x-x') + b$	0.01259	

Table 4. Details of the number of blocks per CV class, the parameters of the CV class and its value

Table 5.	Simulation results using the multiclass SVM model compared with simulations using the SVM model without multiclass
	(SVM only), using the original dataset was the reference

Test statistic	SVM model only Multiclass	SVM model
Accuracy counts		
30:70	70.2600000	78.210000
50:50	70.6000000	78.9200000
70:30	73.2100000	79.8800000
MSE	0.0001429	3.242E-05
MAE	0.0098611	0.0046254
MAPE	0.6946638	0.3602532
\mathbb{R}^2	0.9827000	0.9992000
AIC	-4213.8360000	-5209.8460000
BIC	-4200.2000000	-5196.2180000



Fig. 1. Diagram showing the multiclass SVM model with robustness tests using OAA and OAO strategies



Fig. 2. Classification using mean reversion and coefficient of variance algorithm





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Fig. 3. Performance of the multiclass SVM model compared with the original dataset where the plot on the x-axis represents the test data at 2001st to 2049th of the entire datasets

Table 6. Performance comparison of the multiclass SVM model using different input datasets

Input datasets	Hyper-parameter	Training error	Accuracy count (%)
EUR-USD	22.2637271674138	0.000000	100.00
EUR-CNY	23.5910412737328	0.000862	99.78
EUR-RUB	32.3227585244721	0.000000	100.00
EUR-CHF	78.9518027969328	0.000000	100.00

In the parameter selection of the SVM simulation software, we selected Laplacian kernel function and compared the results simulations of the OAA and OAO strategies. **Table 6** presented performance comparison of the multiclass SVM models using the different input datasets. The Accuracy count for the OAA and OAO strategies reached to 100% for every single simulated input data except EUR-CNY yielded 99.78% and the training errors of each simulation were similar.

4. DISCUSSION

The mechanism of mean reversion and coefficient of variance algorithm started by classifying each datasets with its mean, giving two separated groups, termed to 'mean₁+' and 'mean₁–'; and continue to divide each mean₁+' and 'mean₁–' until the minimum and maximum values of the datasets located in both ends. Therefore, we may obtain 'mean₂+' and 'mean₂–' inasmuch as 'mean₃+' and 'mean₃–' and so on. In this study, we optimise the classification process; and have found six possible CV classes. The future work will be in the area of optimization of kernel functions in the frequency domain.

5. CONCLUSION

The multiclass algorithm for SVM model consists of mean reversion and coefficient of variance algorithm using for partition and classification nonlinear nonstationary datasets yields a significant outcome, compared with the conventional SVM model without multiclass algorithm. To verify the robustness of the proposed algorithm, the OAA and OAO strategies were introduced. By using a variety of test statistic, the simulation results using different inputs from many exchange rates i.e., EUR-USD, EUR-CNY, EUR-RUB and EUR-CHF confirmed that the proposed multiclass algorithm outperformed significantly the simulations of the conventional SVM model.

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7. REFERENCES

- Allwein, E.L., R.E. Schapire and Y. Singer, 2000. Reducing multiclass to binary: A unifying approach for margin classifiers. J. Mach. Learn. Res., 1: 113-141. DOI: 10.1162/15324430152733133
- Bali, T.G. and K.O. Demitras, 2008. Testing mean reversion in stock market volatility. J. Futures Markets, 28: 1-33.
- Chen, J., C. Wang and R. Wang, 2009. Adaptive binary tree for fast SVM multiclass classification. Neurocomputing, 72: 3370-3375. DOI: 10.1016/j.neucom.2009.03.013
- Chen, S.N. and K. Jeon, 2000. Mean reversion behavior of the returns on currency assets. Int. Rev. Econ. Finance, 7: 185-200. DOI: 10.1016/S1059-0560(98)90039-9
- Cieslak, D.A. and N.V. Chawla, 2009. A framework for monitoring classifiers' performance: When and why failure occurs? Knowl. Inform. Syst., 18: 83-109. DOI: 10.1007/s10115-008-0139-1
- Cochrane, J.H., 1988. How big is the random walk in GNP. J. Political Econ., 96: 893-920. DOI: 10.1086/261569
- Datig, M. and T. Schlurmann, 2004. Performance and limitations of the Hilbert-Huang Transformation (HHT) with an application to irregular water waves. Ocean Eng., 31: 1783-1834. DOI: 10.1016/j.oceaneng.2004.03.007
- Diebold, F.X., 2004. The nobel memorial prize for robert f. engle. Scandinavian J. Econ., 106: 165-185.
- Dietterich, T.G. and G. Bakiri, 1995. Solving Multiclass Learning Problems via Error-Correcting Output Codes. J. Arti Intell. Res., 2: 263-286. DOI: 10.1613/jair.105
- Fama, E.F. and K.R. French, 1992. The cross-section of expected stock returns. J. Finance, 47: 427-465. DOI: 10.2307/2329112
- Guhathakurta, K., I. Mukherjee and A. Roy, 2008. Empirical mode decomposition analysis of two different financial time series and their comparison. Chaos. Solut. Fractals, 37: 1214-1227. DOI: 10.1016/j.chaos.2006.10.065
- Hsu, C.W. and C.J. Lin, 2002. A comparison of methods for multiclass support vector machines. IEEE Trans. Neural Netw., 13: 415-425. DOI: 10.1109/72.991427
- Huang, N.E. and N.O. Attoh-Okine, 2005. The Hilbert Transform in Engineering. 1st Edn., CRC Press, ISBN-10: 0849334225, pp: 328.

- Huang, N.E., Z. Shen and S.R. Long, M.C. Wu and H.H. Shih *et al.*, 1998. The empirical mode decomposition and the hilbert spectrum for nonlinear and nonstationary time series analysis. Proc. R Soc. Lond. A., 454: 903-995. DOI: 10.1098/rspa.1998.0193
- Huang, N.N.E. and S.S.P. Shen, 2005. Hilbert-Huang Transform and Its Applications. 1st Edn., World Scientific Publishing, Hackensack, ISBN-10: 9812563768, pp: 311.
- Huang, W., Z. Shen, N.E. Huang and Y.C. Fung, 1996. Nonlinear indicial response of complex nonstationary oscillations as pulmonary hypertension responding to step hypoxia. Proc. Nat. Acad. Sci., 96: 1834-1839. DOI: 10.1073/pnas.96.5.1834
- Kim, D. and H.S. Oh, 2012. EMD: Empirical Mode Decomposition and Hilbert Spectral Analysis.
- Lo, A.W and A.C. MacKinlay, 1988. Stock market prices do not follow random walks: Evidence from a simple specification test. Rev. Financ. Stud., 1: 41-66. DOI: 10.1093/rfs/1.1.41
- Pillay, E. and J.G. O'Hare, 2011. FFT based option pricing under a mean reverting process with stochastic volatility and jumps. J. Comput. Applied Math., 12: 3378-3384. DOI: 10.1016/j.cam.2010.10.024
- Poterba, J.M. and L.H. Summers, 1988. Mean reversion in stock prices: Evidence and implications. J. Financ. Econ., 22: 27-59. DOI: 10.1016/0304-405X(88)90021-9
- Rifkin, R. and A. Klautau, 2004. In defense of one-vs-all classification. J. Mach. Learn. Res., 5: 101-141.
- Schneider, J. and A. Moore, 1997. A Locally Weighted Learning Tutorial using Vizier 1.0. Carnegie Mellon University.
- Shi, F., Q.J. Chen and N.N. Li, 2008. Hilbert Huang transform for predicting proteins subcellular location. J. Biomed. Sci. Eng., 1: 59-63. DOI: 10.4236/jbise.2008.11009
- Uhlenbeck, G.E. and L.S. Ornstein, 1930. On the Theory of the Brownian Motion. Phy. Rev., 36: 823-841. DOI: 10.1103/PhysRev.36.823
- Wang, L., C. Koblinsky, S. Howden and N.E. Huang, 1990. Interannual variability in the south china sea from expendable bathythermograph data. J. Geophys. Res., 104: 509-523. DOI: 10.1029/1999JC900199
- Zhao, Z.W. D.H. Wang, and Y. Zhang, 2011. Limit theory for random coefficient first-order autoregressive process under martingale difference error sequence. J. Comput. Applied Math., 235: 2515-2522. DOI: 10.1016/j.cam.2010.11.004

