Original Research Paper

Application of Graph Theory Concepts in Computer Networks and its Suitability for the Resource Provisioning Issues in Cloud Computing-A Review

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Corresponding Author: Kanniga Devi Rangaswamy Department of Computer Science and Engineering, Kalasalingam University, Krishnankoil, Tamilnadu, India Email: rkannigadevi@gmail.com **Abstract:** Cloud computing, a kind of web service provisioning model, provides immense benefits over traditional IT service environments with the help of virtualization technology. As cloud computing is not a fully matured paradigm, it poses many open issues to be addressed. The key research problem in cloud computing is efficient resource provisioning which is due to its complex and distributed architecture. Graph-based representations of complex networks provide simpler views and graph theoretical techniques provide simpler solutions for lot of issues inherent in networks. Hence, this paper begins with exploration of graph theory applications in cloud computing. This work pays attention to basic resource provisioning problems arise in cloud computing environments and presents some conceptual graph theoretical suggestions to address these issues.

Keywords: Computer Network, Cloud Computing, Graph Theory, Resource Provisioning

Introduction

The next step in the evolution of distributed computing is cloud computing. It inherits existing distributed computing models such as grid computing, utility computing and adds additional flavour namely virtualization. Large-scale processing and storage of data are very much simplified with the advent of costeffective cloud computing solutions. The Cloud Data Center (CDC) (Wu and Buyya, 2015) is very complex with resources distributed globally leading to several issues. The authors of (Zhang et al., 2010; Smith et al., 2009; Marston et al., 2011; Rimal et al., 2009; Shahzad, 2014) addressed several key and fundamental cloud computing issues like resource provisioning, security, privacy, energy and interoperability, but this list is not limited. From the perspective of cloud service provider and cloud service consumer, these issues provide different pictures. While cloud computing provides opportunities to migrate the IT business services online, these key issues need to be resolved before it is accepted as a successful business model.

This article identifies the opportunities of graph theory (Bondy and Murty, 1976) based solutions for the resource provisioning issues inherent in cloud computing. First, it starts with graph theory applications in various areas in computer networks and then explores its suitability to address the resource provisioning issues of cloud. Graph theory is part of discrete mathematics and useful structure to model relationship between objects. Graph theory mainly finds its applications in network modeling, biology, electrical network, computational algorithms and scheduling. Graph theoretical techniques are highly used by computer science applications especially in modeling and routing in networks. Representing a problem as a graph can provide a different point of view and makes a problem much simpler. It provides tools for solving the problem and set of techniques for analysing graphs.

This work has two main parts. The first part gives an overview of graph theory applications in computer networks. As cloud data center has a set of interconnected systems, graph theoretical solutions on computer networks can well be applied on cloud with suitable modifications to address its issues. The second part gives an overview of graph theory applications in cloud. The main idea behind this work is to find out the scope for applicability of graph theory to address resource provisioning issues in cloud.



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Key Research Issues in Cloud Computing

Resource Provisioning

The authors of (Meng *et al.*, 2010; Buyya *et al.*, 2011; Vecchiola *et al.*, 2012; Javadi *et al.*, 2012; Warneke and Kao, 2011) proposed that unlike traditional resource provisioning where resources are provisioned as it is, cloud demands efficient resource provisioning algorithms to provision virtualized resources to meet SLA requirements. Virtualized data centers are envisioned to provide better management flexibility, lower cost, scalability, better resources utilization and energy efficiency, but virtualization is not an easy task to do.

Security

The authors of (Denz and Taylor, 2013; Ward and Barker, 2014; Mahajan *et al.*, 2011; Subashini and Kavitha, 2011; Zissis and Lekkas, 2012) discussed that as users and corporate information reside on third-party systems, no one can guarantee how secure the data are. It is prone to leakage of information and attack. Security is a primary issue which should be handled by all the cloud service providers to retain their business in the market. They should take steps to protect data and its privacy. Five most representative security and privacy attributes are confidentiality, integrity, availability, accountability and privacy-preservability.

Cost

The authors of (Sahni and Vidyarthi, 2015; Tsai and Liao, 2015; Waibel *et al.*, 2016; Hadji *et al.*, 2016) proposed that the public cloud offers pay per use, which can provide low-cost options for short-term projects. Still, for long-term use, enterprise IT organizations may be better off making a capital investment to purchase additional hardware and software. Enterprises need to conduct a break-even analysis to determine whether a public or private cloud would be more cost-effective for them. From the perspective of provider, they are interested in customer satisfaction and generating revenue out of their services. From the perspective of consumer, they are interested in cost-effective solutions. To balance these two points, cost-effective cloud solutions need to be developed.

Reliability

The authors of (Vishwanath and Nagappan, 2010; Poola *et al.*, 2014; Di and Wang, 2013; Zheng *et al.*, 2012) stated that due to high system complexity and distributed structure, even carefully engineered data centers are subject to a large number of failures. Fault tolerant systems should be built to address reliability concerns. Because of the abstraction nature of cloud environment, there arise a need to develop new or extend traditional fault tolerant approaches. VM migration and Server consolidation are the major threatening factor for fault tolerance as they incur service downtime.

Interoperability

The authors of (Govindrajan and Lakshmanan, 2010; Loutas *et al.*, 2011) stated that interoperability of heterogeneous cloud platforms are difficult because they use distinct hypervisor and VM technologies. The platforms also use various security standards and management interfaces. Multiple vendors with different product standards poses challenges for interoperability. Cloud adoption will be stopped if there is not a good way of integrating data and applications across clouds; hence a unified cloud interface and open standards need to be developed.

Energy

The authors of (Beloglazov *et al.*, 2011; Guo and Fang, 2013; Dayarathna *et al.*, 2016; Beloglazov and Buyya, 2010; Lee and Zomaya, 2010) stated that increasing demand for computational power, leads to setting up large-scale data centers. On the other side, the power consumption of these large-scale data centers is enormous. Hence, design of energy efficient hardware and intelligent resource management techniques is required. Due to enormous power consumption, carbon dioxide (CO₂) emission is also more contributing to the greenhouse effect. Hence number of practices need to be applied to achieve energy efficient, such as improvement of applications' algorithms, energy efficient hardware and energy-efficient resource management strategies on a virtualized data center.

Out of all these above mentioned key issues, this work pays much attention to resource provisioning issue and application of graph theory on it.

Resource Provisioning in Cloud

In cloud computing, resource provisioning (Meng et al., 2010; Buyya et al., 2011; Vecchiola et al., 2012; Javadi et al., 2012; Warneke and Kao, 2011) is the allocation of a cloud data center resources to a user. When cloud data center accepts requests for hardware or software resources, it must create and provision them as virtualized resources. It means the monitoring, dynamic selection/scheduling, deployment/placement and management/load balancing of software and hardware resources for ensuring Service Level Agreement (SLA). The SLA is an agreement between the cloud service provider and the user on guaranteeing Quality of Service (QoS). The provisioning can be done in several different ways. In particular, this work addresses the following aspects of resource provisioning from CDC:

- Efficient monitoring for provisioning CDC resources
- Optimal VM placement and migration in CDC for energy-efficient resource provisioning

- Proper locating of CDCs and allocation of CDCs to the source of requests
- Clustering distributed CDCs for faster server provisioning
- Uniform assignment of clients to CDC servers
- Traffic-aware VM migration to load balance cloud servers

Efficient Monitoring for Provisioning CDC Resources

Task scheduling, load balancing are complicated in cloud computing environment due to its abstract heterogeneous architecture, dynamic behaviour and resource heterogeneity. Monitoring of resources is required before performing scheduling and load balancing.

Optimal VM Placement and Migration in CDC for Energy-Efficient Resource Provisioning

Keeping lot of PMs and VMs running in the datacenter consumes more energy, leading to higher operating costs. Hence identifying physical machines with least load and migrating its load to some other physical machines and then shutting them down saves energy. Conservation of energy may be better achieved through optimal placement of VMs on the PMs and performing VM migrations, so that energy consumption may be maintained at desirable level.

Proper Locating of CDCs and Allocation of CDCs to the Source of Requests

The requests for the CDC services can come from different parts of the world. The term source of requests/clients denote the users who make requests to various cloud data center services. The distance between the cloud data center and the source of requests is a major factor influencing the quality of service in terms of response time and latency. Cloud data center allocation is one of the major issues in cloud computing. An efficient allocation of cloud data center to the source of requests may improve the quality of services.

Clustering Distributed CDCs for Faster Server Provisioning

Normally cloud data centers are distributed across the world to increase the availability of services by remote mirroring, replication which are the kind of redundancy mechanisms. It is distributed mainly for disaster recovery. Clustering region-wise deployed cloud data centers will provide rapid responses.

Uniform assignment of clients to CDC servers

In a distributed cloud data center environment, load balancing techniques direct the requests to the closest source or to the source with the most able capacity to serve the request. Variety of algorithms are used to perform load balancing. But there is a trade-off always exits between choosing the closest cloud data center and balancing the load of cloud data center. Sometimes a cloud data center closer to the user location may be in overloaded condition, during this case, the requests will be routed to a distant cloud data center which is capable of handling the requests. Hence, there arise a need to deal with this trade-off which may consider both proximity and load at the same time.

Traffic-Aware VM Migration to Load Balance Cloud Servers

Upon receiving the load information, cloud broker must invoke load balancing procedure to distribute the load uniform across the hosts in the CDC. It can be done by migrating some of the VMs from overloaded hosts to underloaded hosts considering only server-side constraints. Network-side constraints also need to be considered to enhance the performance of CDCs.

Graph Theory Applications in Computer Networks

This section summary of some of the works, which applied graph theory in various types of computer network.

Table 1 lists some of the possible graph theory applications in various types of network. Since cloud is a kind of network, these traditional graph theoretical techniques can be analyzed for their suitability to address resource provisioning issues in cloud and also presents some conceptual suggestions for it.

Graph Theory Applications in Cloud Computing

This section provides summary of works, which applied graph theory in cloud.

The author of (Çatalyürek et al., 2011) proposed a heuristic based on hypergraph and its partitioning for optimizing scientific workflow execution. The author of (Dai et al., 2009) modeled the reliability of the cloud services. This paper models network failure, overflow failure, timeout failure, resource missing failure, hardware failure, software failure and database failure failures using Markov models, Queuing Theory and Graph Theory. The author of (Verbelen et al., 2013) investigated how to optimally deploy software applications on the offered infrastructure in the cloud, by minimizing the network usage. Especially in the context of mobile computing. They designed and evaluated graph partitioning algorithms that allocate software components to machines in the cloud while minimizing the required bandwidth. The author of (Li et al., 2012) proposed CAM, a cloud platform that provides an innovative resource scheduler particularly designed for hosting MapReduce applications in the cloud.

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Potluri and Ningh (7017) Canacitated dominating set Munimum canacitated dominating Wireless networks				
set construction	Potluri and Singh (2012)	Capacitated dominating set	Minimum capacitated dominating	wireless networks
Bar-Ilan <i>et al.</i> (1992) Facility location problem Locating centers General facility	Don Hop at al (1002)	Easility logation problem		Concerct facility

Table 2: Graph theory in cloud

Author	Graph theory technique	Issue addressed	Limitation
Çatalyürek <i>et al.</i> (2011)	Hypergraph	Modeling cloud network	Scheduling is done in two-phases which increases makespan. If done in single phase, it may minimize the makespan of the
`			workflow. This work didn't consider dynamic workflows whose execution pattern changes over time as well.
Dai et al. (2009)	Spanning tree	Cloud service reliability	Cloud service reliability model and evaluation algorithm have not been validated by simulation and real-life data. They have
Verbelen <i>et al.</i>	Creak a setiti seria s	Coffeense denlemment in	proposed only theoretical model.
(2013)	Graph partitioning	Software deployment in mobile cloud	This work considered only minimizing the bandwidth between software components. It didn't minimize the execution time
(2013)		moone cloud	of tasks. This work provide scope for integrating their algorithms
			to address energy consumption objective.
Li et al. (2012)	Flow network algorithms	Optimizing MapReduce	Validation of min-cost flow model for data and VM placement
El ci ul. (2012)	-Ford-Fulkerson	performance in cloud	is to be done in larger real VM clusters.
Binz et al. (2012)	Topological graph theory	Topology management	Enterprise Topology Graph (ETG) is to be built as reusable
, ,	· · · · · · · · · · · · · · · · · · ·	in cloud	building blocks to address specific problem domains with
			broad set of basic operations.
Bansal et al. (2011) Graph mapping	Congestion minimization	Only mapping of two classes of workloads, namely depth-d
		in cloud network	trees and complete graph are considered.
Chan et al. (2009)	Predicate-based graph	Modeling and Testing	This model supports only stateless atomic operations expressed
		cloud	in context free grammar. Some other attributes such as scalability,
			exception handling, dynamic binding, service interactions can also
			be considered to make the model valuable.
Peng et al. (2015)	Graph cut theory	Virtual Machine (VM)	Time taken for VM clustering is a valuable parameter, which
		clustering in cloud	is not mentioned. Not mentioned the applicability of
Zegzhda and	Graph model	Security model for VM	hypervisor security model on the specific type of hypervisor
Nikolsky (2014)		hypervisor in cloud	architectures, namely hosted or bare-metal.

CAM uses a flow-network-based algorithm that is able to optimize MapReduce performance under the specified constraints. The author of (Binz et al., 2012) proposed Enterprise Topology Graphs (ETG) as formal model to describe an enterprise topology. The author of (Bansal et al., 2011) represented the physical network of the cloud as a graph considering the objective of minimizing the congestion. The author of (Chan et al., 2009) formulated a computing cloud as a kind of graph, a computing resource such as services or intellectual property access rights as an attribute of a graph node and the use of the resource as a predicate on an edge of the graph. It also proposes to model cloud computation as a set of paths in a subgraph of the cloud such that every edge contains a predicate that is evaluated to be true. Finally, it presents a set of algorithms to compose cloud computations and model-based testing criteria to test cloud applications. The author of (Peng et al., 2015) constructed a method for VM cluster by energy minimization based on graph theory. Then, they changed deployment of VM cluster into maximum flow minimum cut problem and finally cut formed for VM cluster. The author of (Zegzhda and Nikolsky, 2014) described a formal security model for virtual machine hypervisors in cloud systems based on the graph theory.

From Table 2, it is observed that only a very minimal literature is available on graph theory applications in cloud and most of these works overlooked its application on resource provisioning. Thus, it opens lot of opportunities to apply graph theoretical techniques to address resource provisioning issues in cloud.

The following section presents some conceptual suggestions for applying graph theory for resource provisioning issues in cloud computing.

Some Conceptual Suggestions for the Suitability of Graph Theory Techniques for Addressing Resource Provisioning in Cloud

This section considers some of the graph theoretical techniques from Table 1 and suggests the following aspects of resource provisioning in cloud and the suitability of such graph theoretical models and techniques to address its issues.

How to Perform Efficient Monitoring for Provisioning CDC Resources?

Monitoring the complex, distributed cloud architecture for tracking resource status is a challenging task. Monitoring ensures the availability of resources before performing successful provisioning. Generally, a central monitor keeps track of the resources in cloud (Galstad, 2016).

The monitor has to query all the resources in the network periodically to get their availability status,

which increases network/message overhead. To resolve this, this work suggests to represent cloud as a graph and construct a minimum dominating set structure, which can be used for monitoring resource status. The minimum dominating set structure can minimize the number of message updates made to the monitor and minimize the update time compared to traditional monitoring methods.

How to Perform Optimal VM Placement and Migration in CDC for Energy-Efficient Resource Provisioning?

As VM placement has direct impact on the performance of the CDC, this work suggests to optimize VM placement and VM migration for energy-efficient resource provisioning. For optimal VM placement, it suggests to construct KD-tree structure of cloud servers and VMs will be placed on best-fit cloud servers quickly. This KD-tree is a useful structure when search involves a multidimensional search key and it is known as associative search. KD-tree is defined as a tree for storing the values or objects in multidimensional space. They scale well in high dimensions. All the resource dimensions namely CPU, RAM, storage and bandwidth of cloud servers and VM can well be represented using KD-tree structure. Moreover, this structure helps in identifying least loaded PMs easily so that VMs running on it can be migrated to other cloud servers and powered off to conserve energy. The author of (Mandal and Khilar, 2013) constructed one dimensional Binary Search Tree, which considers only single resource dimension, CPU.

How to Ensure Proper Locating of CDCs and Allocation of CDCs to the Source of Requests?

This suggests to model cloud data center network as a graph and use facility location problem to locate CDCs in appropriate locations to serve the source of requests. Limiting the distance between cloud data centers and the source of requests leads to faster service provisioning. The author of (Doyle et al., 2013) has proposed the source of requests assignment to the closest cloud data center to reduce the carbon emission but they modeled cloud data center as a complete graph which is unrealistic. They modelled both the networking and computational components of the infrastructure as a graph and proposed a system which utilizes Voronoi partitions to determine how source requests to be routed to appropriate data center based on the relative priorities of the cloud operator for latency purposes. The author of (Bar-Ilan et al., 1992) provided solutions for facility location problems. They have considered distributing the clients to centers as balanced as possible, but they have overlooked the distance between clients and centers, which is also essential for faster service provisioning.

How to Cluster Distributed CDCs for Faster Server Provisioning?

This suggests to model the cloud environment as a graph and cluster distributed CDCs in order to enable faster service provisioning to the clients. Many works have considered graph-based K-Means (Galluccio *et al.*, 2012) and K-Spanning tree (Zhou *et al.*, 2011) clustering methods to cluster a network. In all these approaches the number of clusters K to be created should be known in advance, but determining K is impractical in case of distributed CDCs. Hence, this work suggests to use dominating set based clustering, where each dominating node acts as a cluster head and neighbors are connected to these cluster heads which makes service provisioning fast. The number of clusters (K) to be created is determined based on size of the graph. So, it leads to a non-constrained clustering algorithm.

How to Ensure Uniform Assignment of Clients to CDC Servers?

This work suggests to use capacitated dominating set concept (Potluri and Singh, 2012) to assign clients to CDC servers. The capacitated dominating set is the problem of finding a dominating set with the additional constraint that the nodes dominated do not exceed the capacity of the dominating node. The capacity can be uniform across all nodes or variable. Hence, a uniform capacity can be assigned to a homogeneous CDC environment and a variable capacity can be assigned to a heterogeneous CDC environment. For client assignment to CDCs, exiting methods have used Round Robin (Radojević and Žagar, 2011) and its variant approaches, which may not guarantee uniformity all the times.

How to Efficiently Perform Traffic-Aware VM Migration to Load Balance Cloud Servers?

Network flow problem (Nakayama and Koide, 2013) in the form of Maximum flow and Minimum cut problem finds its application in various fields ranging from checking network connectivity, network reliability, namely a few.

This work suggests to use network flow problem by converting cloud into a flow network and to perform traffic-aware live VM migration in order to load balance the cloud servers. Most of the existing benchmarked VM migration approaches (Khanna *et al.*, 2006; Wood *et al.*, 2007) consider only host-side resource constraints with little consideration on network-side constraints. A good VM migration algorithm which considers both serverside and network-side constraints can greatly improve their performance. This can be done on both live migration or cold migration scenarios.

In network flow problem, a set of path in a graph G is edge-disjoint if each edge in G appears in at most one path. In cloud, some k number of edge-disjoint paths can be computed between overloaded and underloaded servers and can migrate each VM from overloaded server to underloaded server on one of these k paths to perform fast and traffic-aware VM migrations.

Conclusion and Future Work

In this study, an analysis is done on the application of graph theory concepts in computer networks and its suitability to address resource provisioning issues in cloud. In future, we would like to analyze its scope in other research areas of cloud computing.

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Author's Contributions

Kanniga Devi Rangaswamy: She devised the main conceptual ideas and developed the review framework. She contributed to part of the literature collection and drafted the manuscript in consultation with Murugaboopathi Gurusamy.

Murugaboopathi Gurusamy: He supervised this review work. He contributed to part of the literature collection and to the formalism of review work. He provided critical feedback and helped shape the research and manuscript.

Ethics

This research manuscript is original and the manuscript is not published elsewhere. The corresponding author ensure that all authors have read and approved the manuscript and no ethical issues involved.

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